

Lecture 31

CS 6260 Automated Planning and Learning

FOND Planning

Department of Computer Science and Engineering

Indian Institute of Technology Madras



Recap: Classical Planning

State-transition system or classical planning domain:

$\Sigma = (S, A, T, \text{cost})$ or (S, A, T)

- S - finite set of *states*
- A - finite set of *actions*
- $T: S \times A \rightarrow S$

prediction (or state-transition) function

- *partial function*: $T(s, a)$ is not necessarily defined for every (s, a)
- a is *applicable* in s iff $T(s, a)$ is defined
- $\text{Domain}(a) = \{s \in S \mid a \text{ is applicable in } s\}$
- $\text{Range}(a) = \{T(s, a) \mid s \in \text{Domain}(a)\}$
- $C: S \times A \rightarrow \mathbb{R}^+$ or $C: A \rightarrow \mathbb{R}^+$
 - optional; default is $\text{cost}(a) \equiv 1$
 - money, time, something else

- *plan*: a sequence of actions $\pi = \langle a_1, \dots, a_n \rangle$
- π is *applicable* in s_0 if the actions are applicable in the order given

$$T(s_0, a_1) = s_1$$

$$T(s_1, a_2) = s_2$$

...

$$T(s_{n-1}, a_n) = s_n$$

- In this case define $T(s_0, \pi) = s_n$, and $\hat{T}(s_0, \pi) = \langle s_1, \dots, s_n \rangle$
- *Classical planning problem*:
 - $P = (\Sigma, s_0, S_g)$
 - planning domain, initial state, set of goal states
- *Solution for P* :
 - a plan π such that $T(s_0, \pi) \in S_g$

FOND Planning*

State-transition system or classical planning

domain: $\Sigma = (S, A, T)$ or (S, A, T)

- S - finite set of states
- A - finite set of actions
- $T: S \times A \times S$

prediction (or state-transition) function

- *partial function*: $T(s, a, s')$ is not necessarily defined for every (s, a, s')
- a is *applicable* in s iff $T(s, a, s')$ is defined
- $\text{Domain}(a) = \{s \in S \mid a \text{ is applicable in } s\}$
- An action is nondeterministic if $|\text{EXEC}(s, a)| > 1$.

- *FOND planning problem*:

- $P = (\Sigma, s_0, S_g)$
- planning domain, initial state, set of goal states

- *Solution for P* :

- a *policy* π

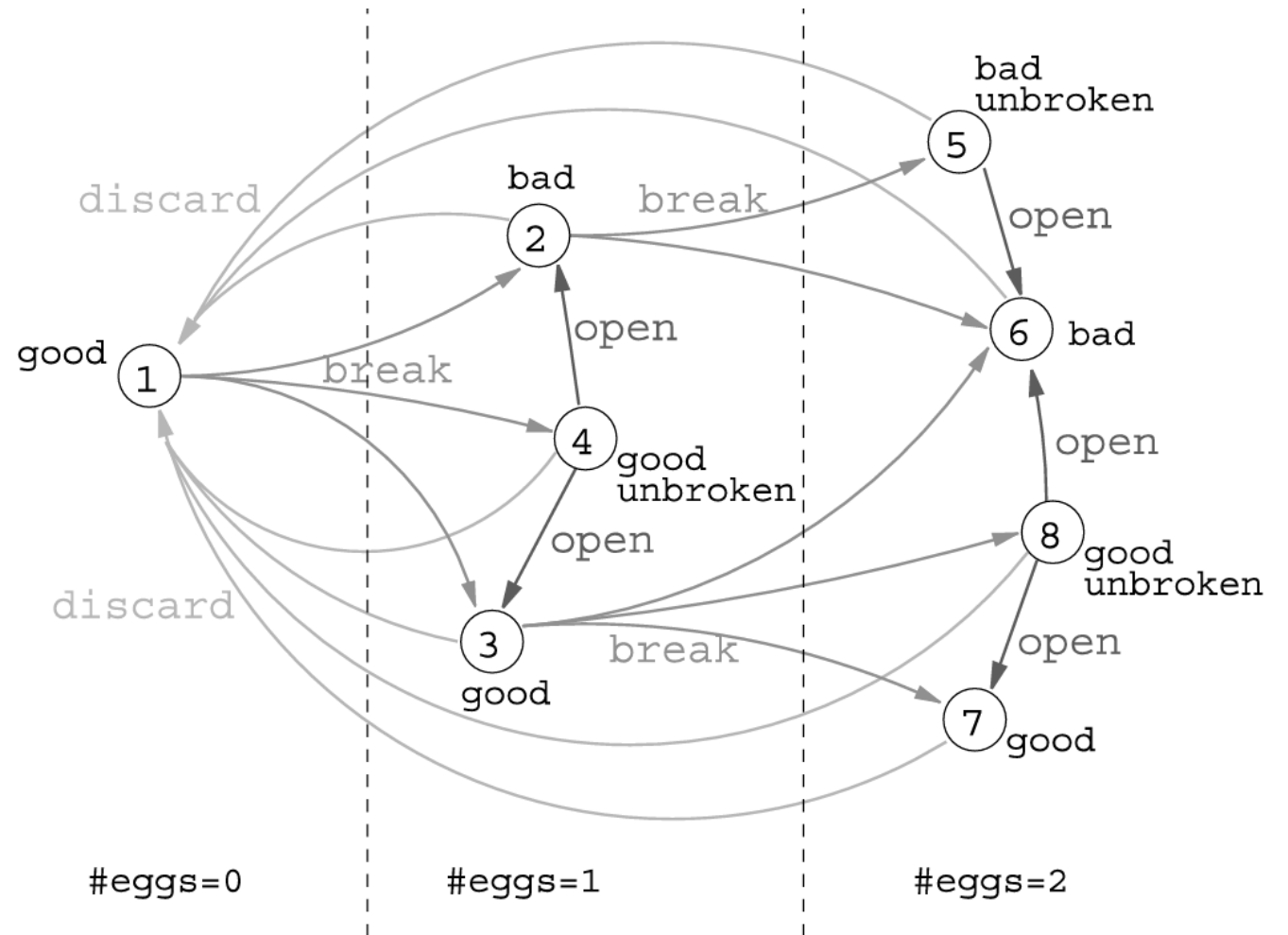
* [Cimatti et al., Weak, strong, and strong cyclic planning via symbolic model checking, Artificial Intelligence, Vol. 147, Iss. 1–2, 2003.](#)

FOND Planning: Action Properties

- $\text{ACT}(s) = \{a : \exists s'. T(s,a,s')\}$
- $\text{EXEC}(s,a) = \{s' : T(s,a,s')\}$
- An action is nondeterministic if $|\text{EXEC}(s,a)| > 1$.
- An action is deterministic if $|\text{EXEC}(s,a)| = 1$.

Running Example: Omelette Preparation

- Propositions P:
 $\{\#eggs=0, \#eggs=1, \#eggs=2, \text{bad}, \text{good}, \text{unbroken}\}$
- State S: 2^P
- Actions: $\{\text{break}, \text{open}, \text{discard}\}$



Naïve Solution Algorithm

```
 $s := \text{SENSECURRENTSTATE}();$   
while  $s \in \text{STATESOF}(\pi)$  do  
     $a := \text{GETACTION}(s, \pi);$   
    EXECUTE( $a$ );  
     $s := \text{SENSECURRENTSTATE}();$   
done
```

FOND Actions: break-first-egg

```
(:action break-first-egg
  :precondition (and
    (eggs-0)
    (not (unbroken))
  )
  :effect (oneof
    ;; Outcome 1: egg breaks cleanly and is good
    (and (not (eggs-0)) (eggs-1) (good) (not (bad)))

    ;; Outcome 2: egg breaks cleanly and is bad
    (and (not (eggs-0)) (eggs-1) (not (good)) (bad))

    ;; Outcome 3: egg fails to break open (still unknown good/bad)
    (and (not (eggs-0)) (eggs-1) (good) (unbroken))
  )
)
```

FOND Actions: break-second-egg

```
(:action break-second-egg
  :precondition (and
    (eggs-1) (good) (not (unbroken))
  )
  :effect (oneof
    ;; Outcome 1: second egg breaks cleanly and is good
    (and (not (eggs-1)) (eggs-2) (good))

    ;; Outcome 2: second egg breaks cleanly and is bad
    (and (not (eggs-1)) (eggs-2) (not (good)) (bad))

    ;; Outcome 3: second egg fails to break open
    (and (not (eggs-1)) (eggs-2) (good) (unbroken))
  )
)
```


FOND Actions: open-egg

```
(:action open-egg
  :precondition (and
    (unbroken)
  )
  :effect (oneof
    ;; Outcome 1 forced-open egg turns out good
    (and (not (unbroken)) (good))

    ;; Outcome 2: forced-open egg turns out bad
    (and (not (unbroken)) (not (good)) (bad))
  )
)
```

```
(:action discard
  :precondition (or
    (eggs-1) (eggs-2)
  )
  :effect (and
    (eggs-0)
    (not (eggs-1)) (not (eggs-2))
    (not (good)) (not (bad)) (not (unbroken))
    (bowl-empty)
  )
)
```

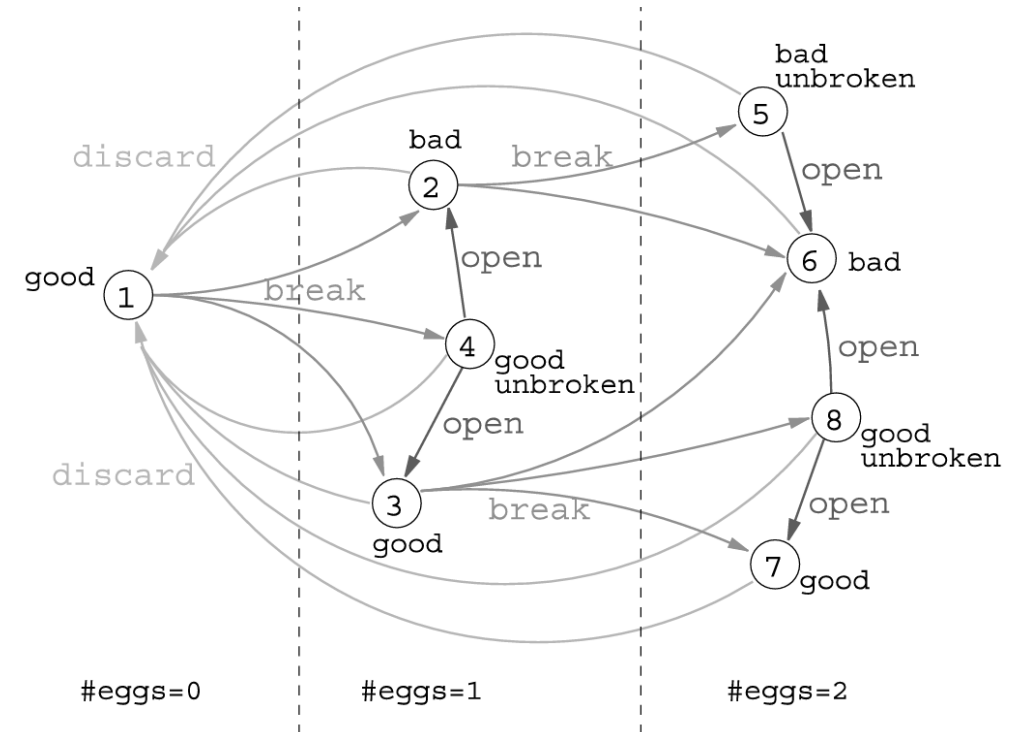
FOND Problem

```
(define (problem omelette-goal)
  (:domain omelette)
  (:init
    eggs-0)
    (good)
    (bowl-empty)
  )

  ;; Goal: two good eggs in the bowl, no bad ones
  (:goal
    (and (eggs-2) (good) (not (bad)) (not (unbroken))))
  )
)
```

State Action Table

- A state-action table π is a set of pairs $\langle s, a \rangle$ where $s \in S$ and $a \in \text{ACT}(s)$. It is deterministic if at most one action is associated with each state. It serves as a reactive policy — the agent senses the world and picks an action at each step.



$$\pi_a \doteq \{ \langle 1, \text{break} \rangle, \langle 3, \text{break} \rangle \},$$

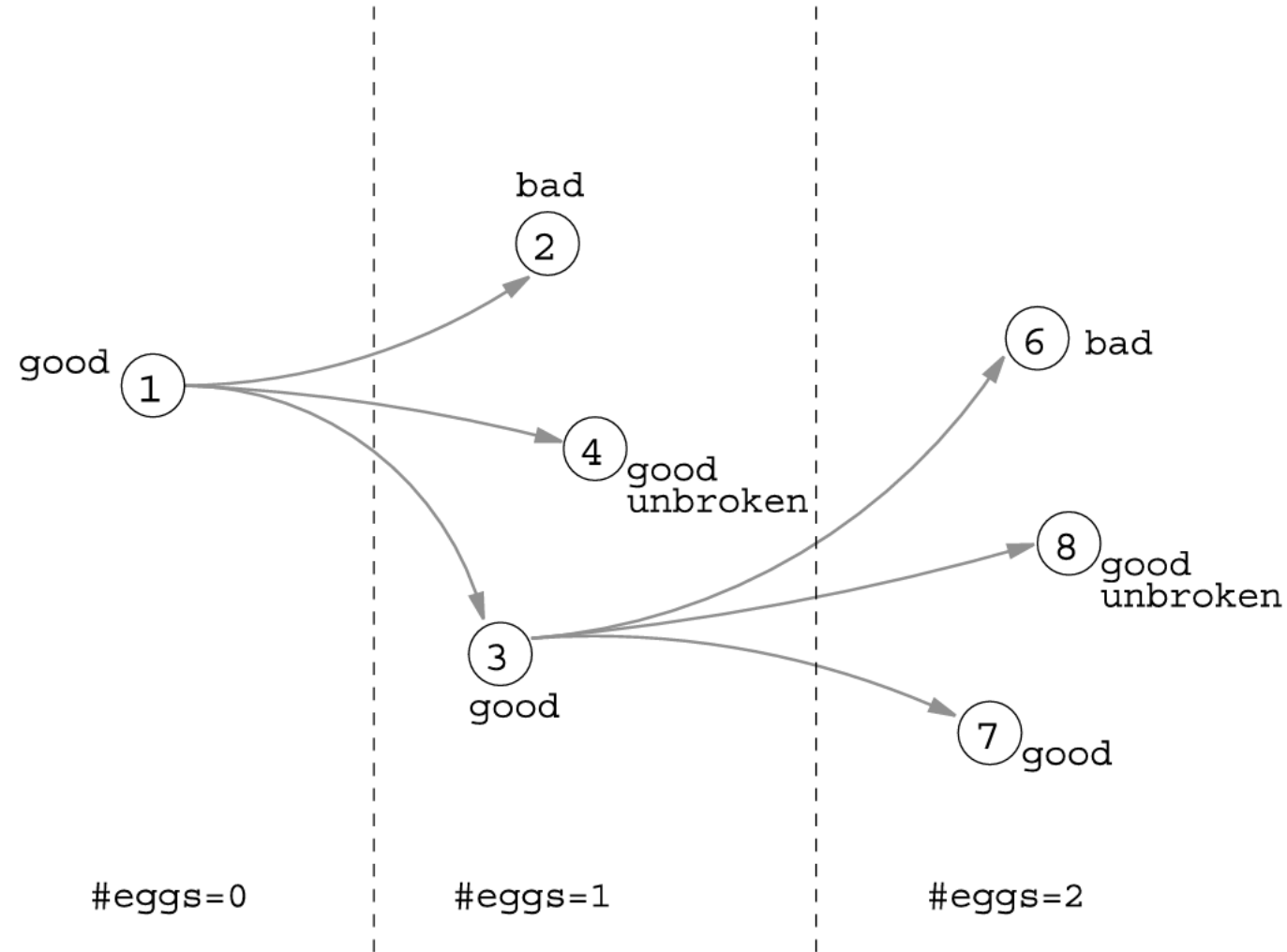
$$\pi_b \doteq \{ \langle 1, \text{break} \rangle, \langle 2, \text{break} \rangle, \langle 3, \text{break} \rangle, \langle 4, \text{open} \rangle, \langle 5, \text{open} \rangle, \langle 8, \text{open} \rangle \}.$$

$$\pi_c \doteq \{ \langle 1, \text{break} \rangle, \langle 2, \text{discard} \rangle, \langle 3, \text{break} \rangle, \langle 4, \text{open} \rangle, \langle 6, \text{discard} \rangle, \langle 8, \text{open} \rangle \}.$$

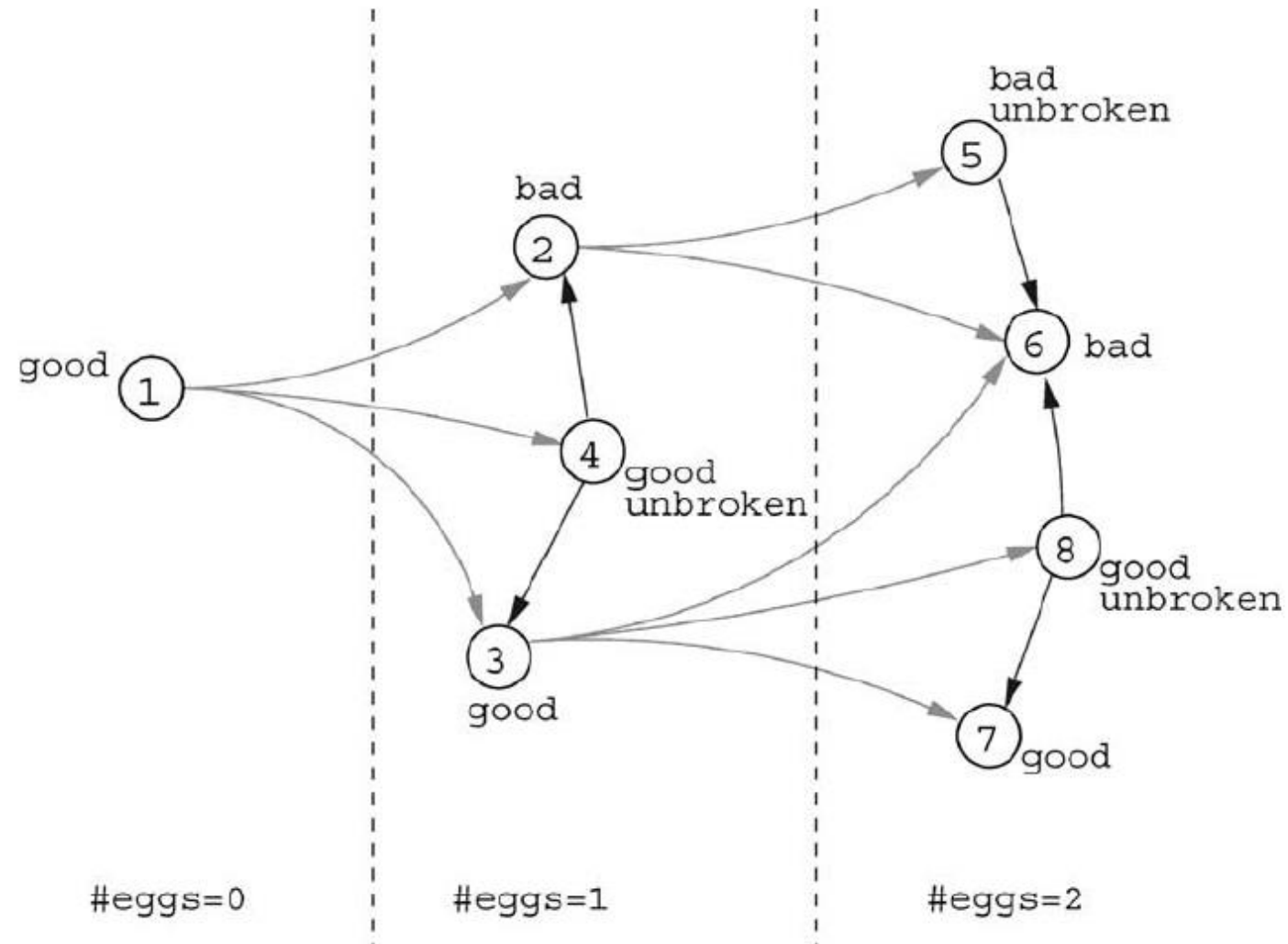
Execution Structure

- Let π be a state-action table of a planning domain D
The execution structure induced by π from the set of initial states $I \subseteq S$ is a tuple $K = \langle Q, L \rangle$, where $Q \subseteq S$ and $L \subseteq S \times S$ are the minimal sets satisfying the following rules:
 1. if $s \in I$, then $s \in Q$, and
 2. if $s \in Q$ and there exists a state-action pair $s, a \in \pi$ such that $T(s, a, s')$, then $s' \in Q$ and $L(s, s')$.
- A state $s \in Q$ is a terminal state of K if there is no $s' \in Q$ such that $T(s, s')$.

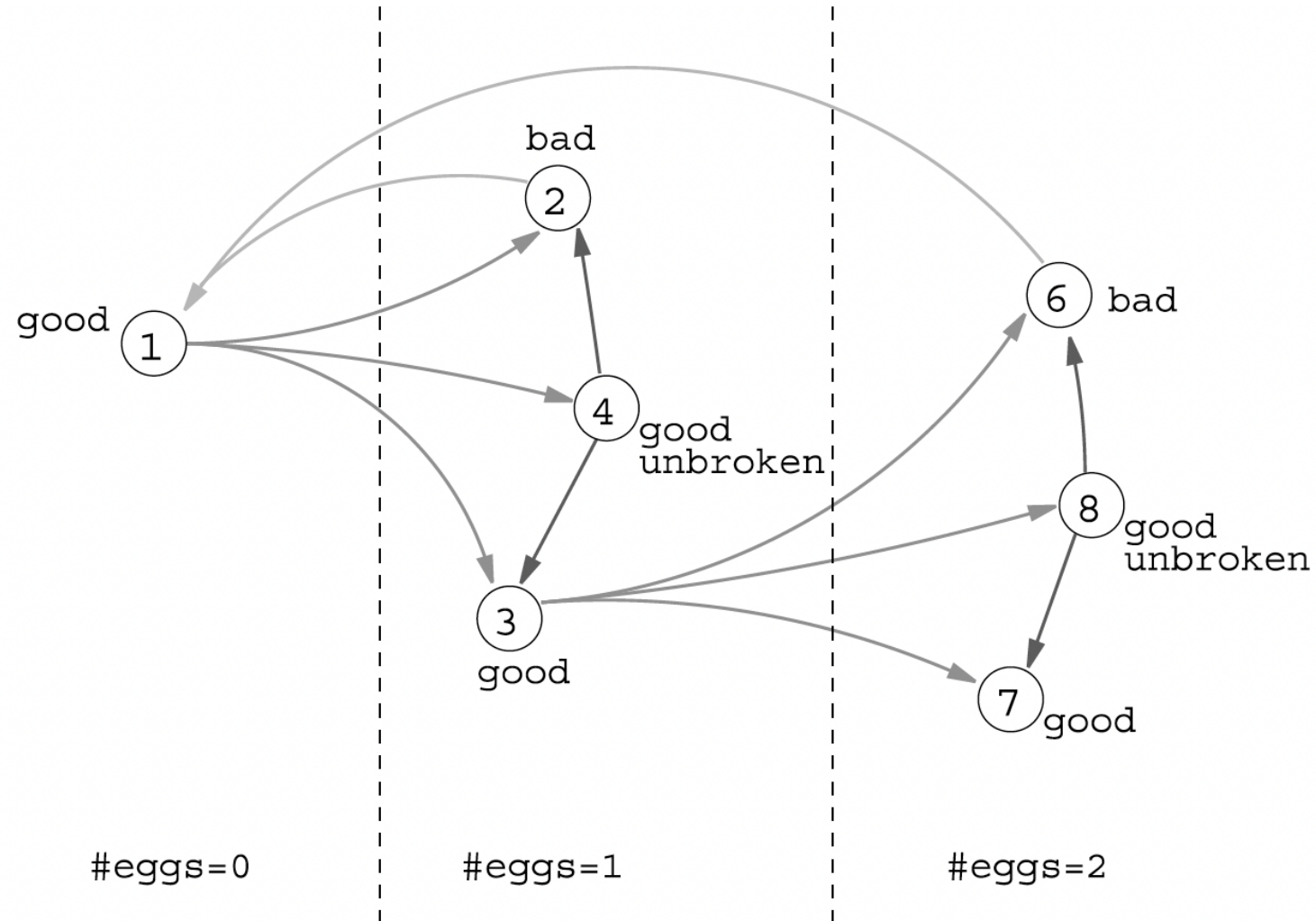
Execution Structure: π_a



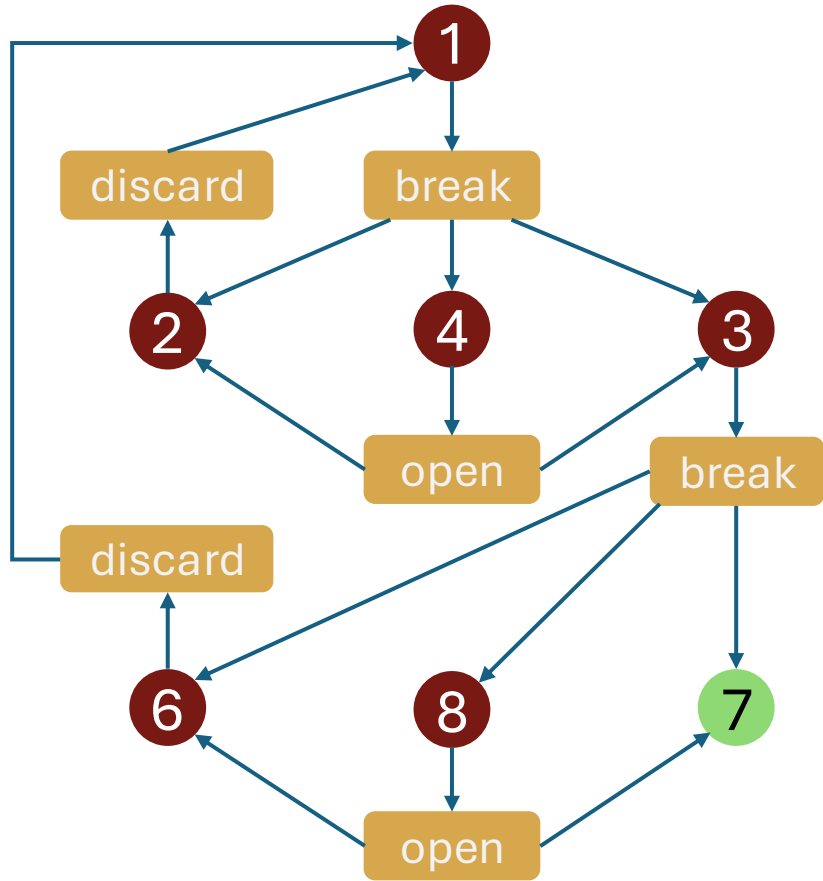
Execution Structure : π_b



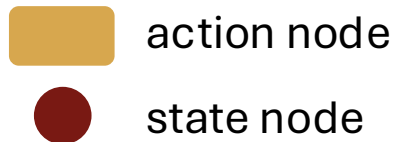
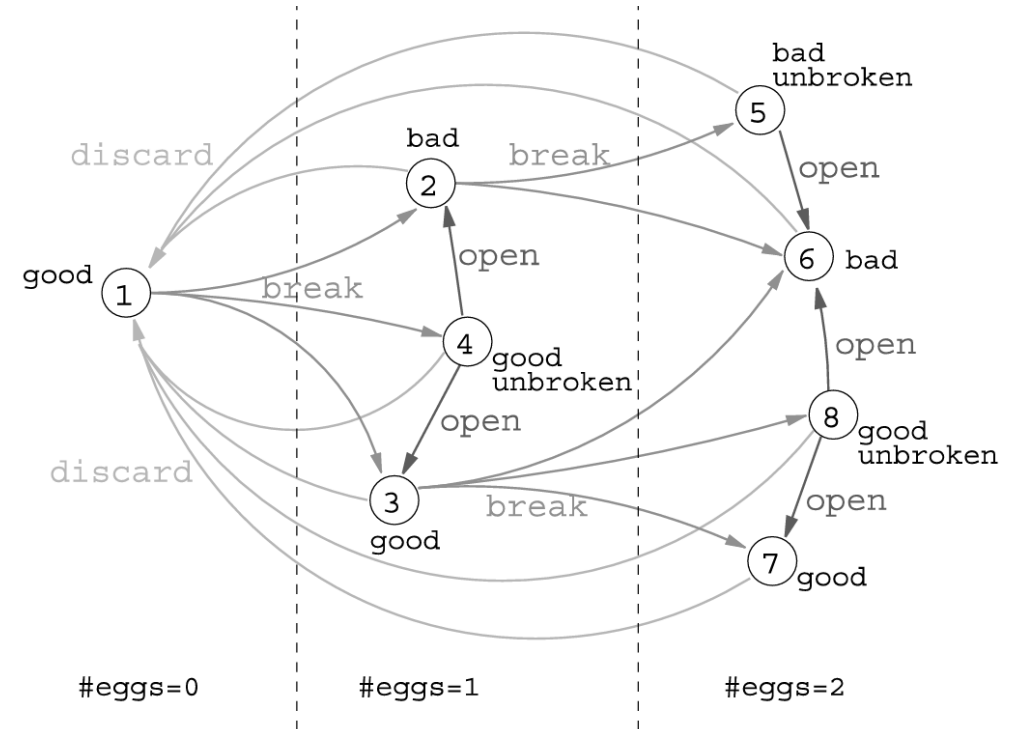
Execution Structure : π_c



Solution Policy



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Solution Policy Properties

Weak Solution

π is weak if for any $s \in I$, some terminal state of K reachable from s is in G .

Strong Solution

π is strong if K is acyclic and ALL terminal states of K are in G .

Strong Cyclic Solution

π is strong cyclic if from every $s \in Q$ some terminal state of K is reachable and all terminal states are in G .

* [Cimatti et al., Weak, strong, and strong cyclic planning via symbolic model checking, Artificial Intelligence, Vol. 147, Iss. 1–2, 2003.](#)

FOND Planner and Additional Material

- PRP Planner: <https://cdn.aaai.org/ojs/13520/13520-40-17038-1-2-20201228.pdf>
- FOND Domains: <https://github.com/AI-Planning/fond-domains>