

Lecture 12

CS 6260 Automated Planning and Learning

Hierarchical Task Networks (HTNs)

Department of Computer Science and Engineering

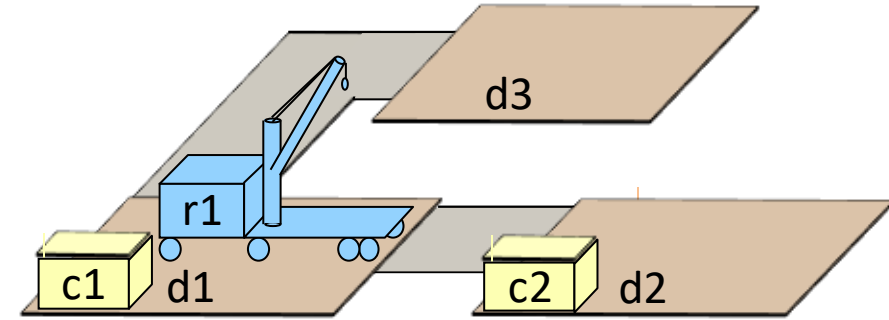
Indian Institute of Technology Madras



Recap: State-Variable Representation

State-Variable Representation

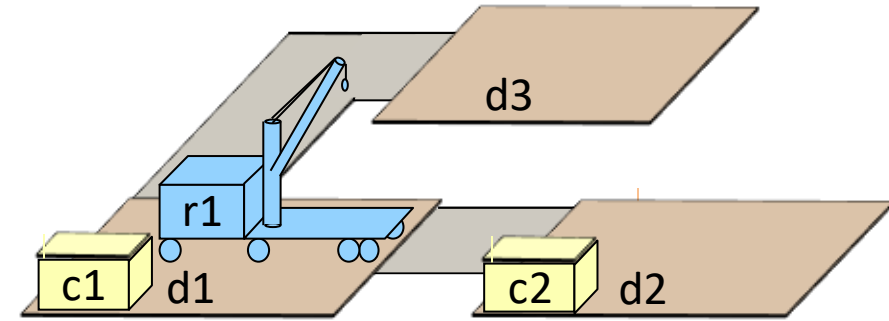
- *Objects* = {names of objects in the environment}
- Organized into a *typed ontology*
 - sets of object types
- *Objects* = *Robots* $\cup$ *Containers* $\cup$ *Locs* $\cup$ {nil}
 - *Robots* = {r1}
 - *Containers* = {c1, c2}
 - *Locs* = {d1, d2, d3}
- *Objects* only needs to include objects that matter at the current level of abstraction
- Can omit lots of details
 - physical characteristics of robots, containers, loading docks, roads, ...
- Objects have two kinds of properties
 - *rigid* and *varying*



States as Functions

- Represent each state s as a function that assigns values to state variables
 - For each state variable x , $s(x)$ is one x 's possible values

$$\begin{aligned}s_1(\text{loc}(r1)) &= d1, & s_1(\text{cargo}(r1)) &= \text{nil}, \\ s_1(\text{loc}(c1)) &= d1, & s_1(\text{loc}(c2)) &= d2\end{aligned}$$



- Mathematically, a function is a set of ordered pairs
$$s_1 = \{(\text{loc}(r1), d1), (\text{cargo}(r1), \text{nil}), (\text{loc}(c1), d1), (\text{loc}(c2), d2)\}$$
- Equivalently, write it as a set of *ground positive literals* (or *ground atoms*):

$$s_1 = \{\text{loc}(r1)=d1, \text{cargo}(r1)=\text{nil}, \text{loc}(c1)=d1, \text{loc}(c2)=d2\}$$

- Here, '=' is a predicate symbol
- Assignment will be indicated with '←'

Suppose $r1$ can move between locations. What does the state need to include to represent that $\text{move}(r1, d1, d2)$ is valid while $\text{move}(r1, d2, d3)$ is invalid?

(short answer)

HTN Planning

HTN Planning

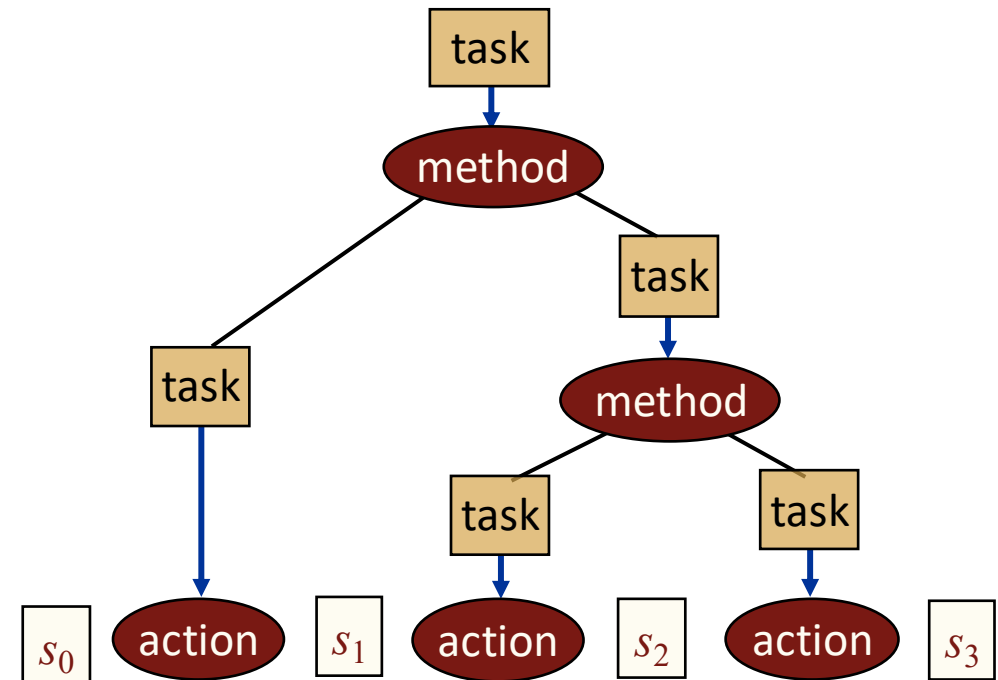
- For some planning problems, we may already have ideas for how to look for solutions
- Example: travel to a destination that's far away:
 - Brute-force search: many combinations of vehicles and routes
- Experienced human: small number of “recipes”
 - e.g., flying:
 1. buy ticket from local airport to remote airport
 2. travel to local airport
 3. fly to remote airport
 4. travel to final destination

HTN Planning

- Two ways to put such information into a planner:
 - Domain-specific algorithm
 - Domain-independent planning engine + domain-specific planning information
 - HTN planning (this Part)
- Ingredients:
 - state-variable planning domain (Part I)
 - tasks: activities to perform
 - HTN methods: ways to perform tasks

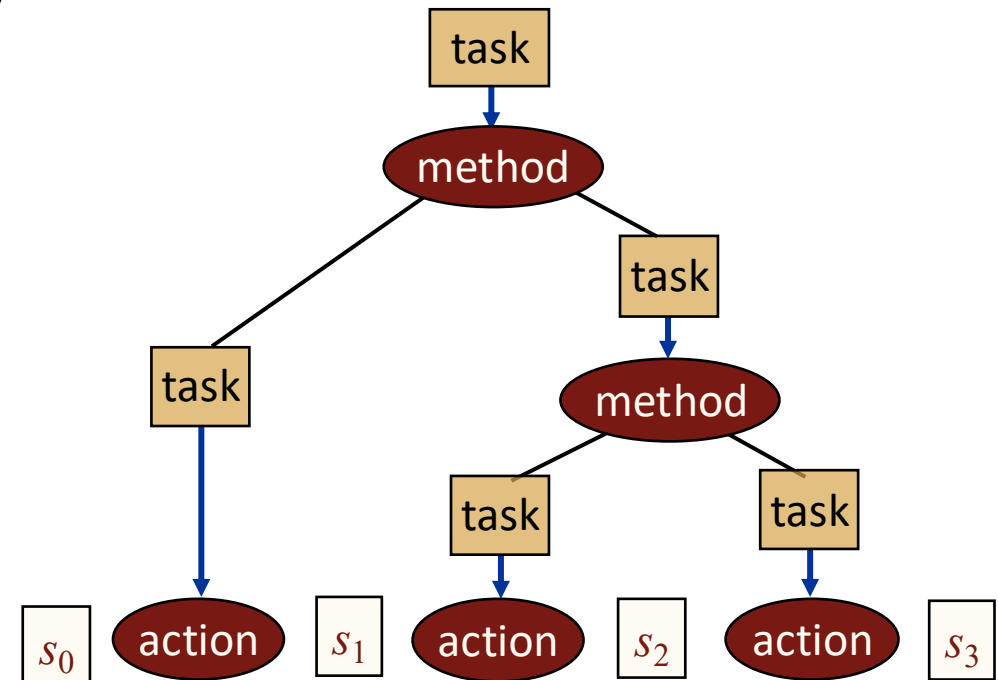
Total-Order HTN Planning: Tasks

- Three kinds of tasks
 - *Primitive task*: head of an action
 - *Compound task*: $name(args)$
 - $name$ is a *compound-task name*
 - *Goal task*: $goal(g)$
 - g is any classical goal formula



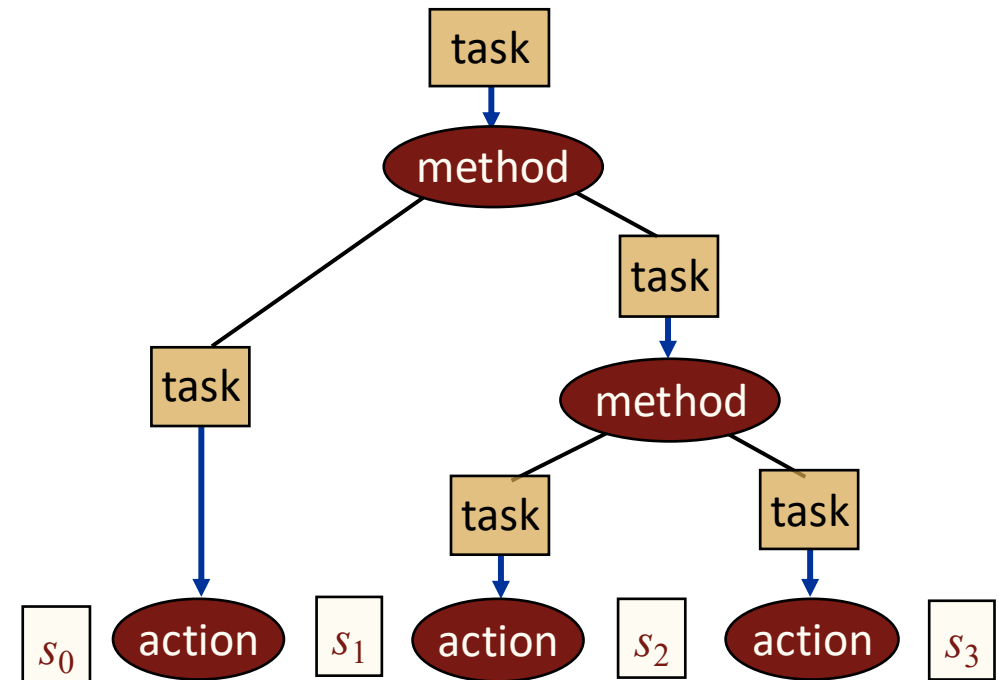
Total-Order HTN Planning: Tasks

- Method: a tuple
 $\langle \text{head}, \text{nonprimitive task}, \text{preconditions}, \text{subtasks} \rangle$
- Write it as pseudocode:
 $\text{method-name}(\text{args})$
 Task: *nonprimitive task*
 Pre: *preconditions*
 Sub: *list of subtasks*



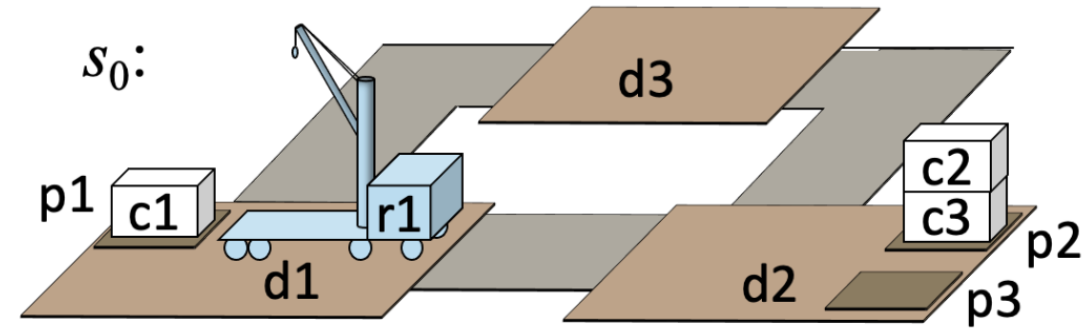
Total-Order HTN Planning

- TOHTN planning domain: a pair $(\Sigma, \mathcal{M})$
 - Σ : state-variable planning domain
 - $\mathcal{M}$: set of methods
- TOHTN planning problem $P = (\Sigma, \mathcal{M}, s_0, T)$
 - $T = \langle t_1, t_2, \dots, t_k \rangle$
- *Solution* for P :
 - any executable plan that can be generated for T by applying
 - methods to nonprimitive tasks
 - actions to primitive tasks



Total-Order HTN Planning

- Objects:
 - robots r1, r2
 - loading docks d1, d2, d3
 - containers c1, c2, c3
 - piles p1, p2, p3
- Rigid relations:
 - adjacent = {(d1,d2), (d2,d1), (d2,d3), (d3,d2), (d3,d1), (d1,d3)};
 - at = {(p1, d1), (p2, d2), (p3, d2)}.
- State variables:
 - $\text{cargo}(r) \in \text{Containers} \cup \{\text{nil}\}$
 - $\text{loc}(r) \in \text{Docks}$
 - $\text{occupied}(d) \in \{\text{T}, \text{F}\}$
 - $\text{pile}(c) \in \text{Piles} \cup \{\text{nil}\}$
 - $\text{pos}(c) \in \text{Robots} \cup \text{Containers} \cup \{\text{nil}\}$
 - $\text{top}(p) \in \text{Containers} \cup \{\text{nil}\}$
 - where $r \in \text{Robots}$, $c \in \text{Containers}$, $p \in \text{Piles}$



Ques 2: Complete the state s_0

$s_0 = \{$
 $\text{cargo}(r1) = \text{nil},$
 $\text{loc}(r1) = d1,$
 $\text{occupied}(d1) = \text{T},$
 $\text{occupied}(d2) = \text{F},$
 $\text{occupied}(d3) = \text{F},$
 $\text{pile}(c1) = p1,$
 $\text{pile}(c2) = p2,$
 $\text{pile}(c3) = p2,$
 $\text{pos}(c1) = \text{nil},$
 $\text{pos}(c2) = c3,$
 $\text{pos}(c3) = \text{nil},$
 $\text{top}(p1) = c1,$
 $\text{top}(p2) = c2,$
 $\text{top}(p3) = \text{nil}\}$

Total-Order HTN Planning

Action schemas:

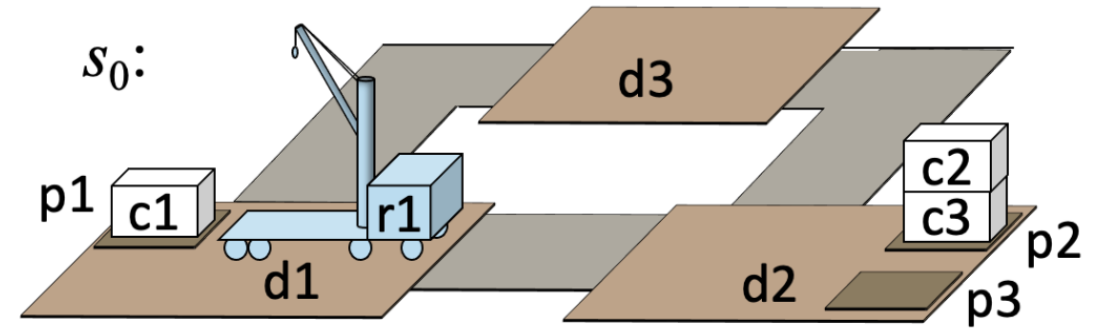
- $\text{take}(r, c, c', p, d)$
 - pre: $\text{at}(p, d)$, $\text{cargo}(r) = \text{nil}$, $\text{loc}(r) = d$, $\text{pos}(c) = c'$, $\text{top}(p) = c$
 - eff: $\text{cargo}(r) \leftarrow c$, $\text{pile}(c) \leftarrow \text{nil}$, $\text{pos}(c) \leftarrow r$, $\text{top}(p) \leftarrow c'$
- $\text{put}(r, c, c', p, d)$
 - pre: $\text{at}(p, d)$, $\text{pos}(c) = r$, $\text{loc}(r) = d$, $\text{top}(p) = c'$
 - eff: $\text{cargo}(r) \leftarrow \text{nil}$, $\text{pile}(c) \leftarrow p$, $\text{pos}(c) \leftarrow c'$, $\text{top}(p) \leftarrow c$
- $\text{move}(r, d, d')$
 - pre: $\text{adjacent}(d, d')$, $\text{loc}(r) = d$, $\text{occupied}(d') = \text{F}$
 - eff: $\text{loc}(r) \leftarrow d'$, $\text{occupied}(d) \leftarrow \text{F}$, $\text{occupied}(d') \leftarrow \text{T}$

where

- $c \in \text{Containers}$; $c' \in \text{Containers} \cup \text{Robots} \cup \{\text{nil}\}$;
- $d, d' \in \text{Docks}$; $p \in \text{Piles}$; $r \in \text{Robots}$.

Ques 3: Notice that $\text{cargo}(r) = c$ iff $\text{pos}(c) = r$. Can we rewrite the domain to eliminate $\text{cargo}(r)$?

A. yes



- State variables:
 - $\text{cargo}(r) \in \text{Containers} \cup \{\text{nil}\}$
 - $\text{loc}(r) \in \text{Docks}$
 - $\text{occupied}(d) \in \{\text{T}, \text{F}\}$
 - $\text{pile}(c) \in \text{Piles} \cup \{\text{nil}\}$
 - $\text{pos}(c) \in \text{Robots} \cup \text{Containers} \cup \{\text{nil}\}$
 - $\text{top}(p) \in \text{Containers} \cup \{\text{nil}\}$

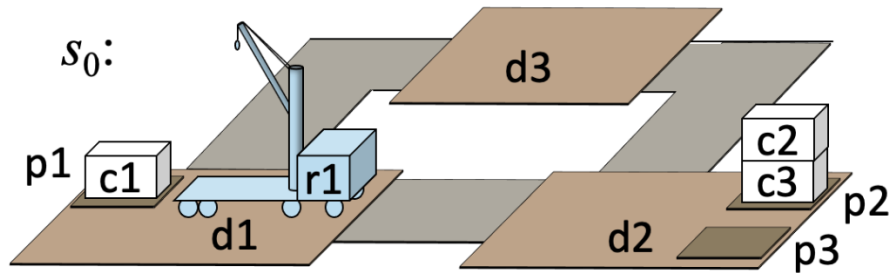
where $r \in \text{Robots}$, $c \in \text{Containers}$, $p \in \text{Piles}$

- $s_0 = \{\text{cargo}(r1) = \text{nil}, \text{cargo}(r2) = \text{nil},$
 $\text{loc}(r1) = d1, \quad \text{loc}(r2) = d2,$
 $\text{occupied}(d1) = \text{T}, \text{occupied}(d2) = \text{F}, \text{occupied}(d3) = \text{F},$
 $\text{pile}(c1) = p1, \quad \text{pile}(c2) = p2, \quad \text{pile}(c3) = p2,$
 $\text{pos}(c1) = \text{nil}, \quad \text{pos}(c2) = c3, \quad \text{pos}(c3) = \text{nil},$
 $\text{top}(p1) = c1, \quad \text{top}(p2) = c2, \quad \text{top}(p3) = \text{nil}\}$

TOHTN Planning Domain

If I say “HTN” assume TOHTN
unless stated otherwise

- TOHTN planning domain $\Sigma = (\Sigma_c, \mathcal{M})$
 - Σ_c = DWR domain on the previous pages
 - $\mathcal{M}$ = a set of eight methods:



- Compound task $\text{put-in-pile}(r, c, p, d)$: put container c into pile p if it isn't there already

```
m1-put-in-pile( $r, c, p, d$ )  
task: {pile( $c$ ) =  $p$ }  
pre: at( $p, d$ ), pile( $c$ )  $\neq p$ , cargo( $r$ ) = nil  
sub: get-container( $r, c$ ), navigate( $r, d$ ), put( $r, c$ , top( $p$ ),  $p, d$ )
```

- Preconditions:
 - 1st one ensures d has the correct value
 - Others check for applicability
- Last subtask: one of the args is a state variable, $\text{top}(p)$
 - Violates a restriction in Chapter 2
 - But many HTN algorithms don't need the restriction

TOHTN Planning Domain (continued)

- Goal task: $\text{goal}(\text{cargo}(r)=c)$
 - Get c onto r
 - Subtask of m2-put-in-pile
- We aren't doing classical planning, so we need a method:

```
m1-get-container( $r, c$ )  
  task: get-container( $r, c$ )  
  pre: cargo( $r$ ) =  $c$   
  sub: // no subtasks
```

```
m2-get-container( $r, c, p, d$ )  
  task: get-container( $r, c$ )  
  pre: cargo( $r$ ) = nil, pile( $c$ ) =  $p$ , at( $p, d$ )  
  sub: navigate( $r, d$ ), uncover( $c$ ),  
       take( $r, c$ , pos( $c$ ),  $p, d$ )
```

- Compound task uncover(c):
 - Subtask of m1-fetch
- Remove any containers that may be piled on top of c

```
m1-uncover( $c$ )  
  task: uncover( $c$ )  
  pre: top(pile( $c$ )) =  $c$   
  sub: // no subtasks
```

```
m2-uncover( $r, c, p, c', p', d$ )  
  task: uncover( $c$ )  
  pre: pile( $c$ ) =  $p$ , top( $p$ ) =  $c'$ ,  $c' \neq c$ ,  
       at( $p, d$ ), at( $p', d$ ),  $p \neq p'$ ,  
       loc( $r$ ) =  $d$ , cargo( $r$ ) = nil  
  sub: take( $r, c'$ , pos( $c'$ ),  $p, d$ ),  
       put( $r, c'$ , top( $p'$ ),  $p', d$ ),  
       uncover( $c$ )
```

Ques4: Can we rewrite m2-uncover to eliminate c' ?

A. yes